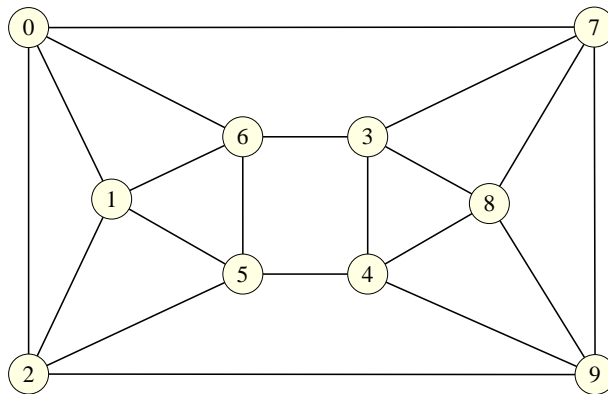


## Exercise Sheet 6

**Issue date:** 19 December 2002      **Hand in by** 14 January 2003  
**Exercise class:** 16 January 2003

**Exercise 6.1:** In the graph drawn below, exhibit a  $k$ -factor for each  $k \in \{0, 1, 2, 3, 4\}$ .



**Exercise 6.2** Determine 1-factorisations of  $K_{4,4}$  and  $K_8$ .

**Exercise 6.3:** For each  $k > 1$ , construct a  $k$ -regular simple graph having no 1-factor.

**Exercise 6.4:** Draw a connected 3-regular simple graph that has a 1-factor and has a cut-vertex. Prove that if the edges of  $G$  can be partitioned into 1-factors, then  $G$  has no cut-vertex.